

# What makes the proton spin?

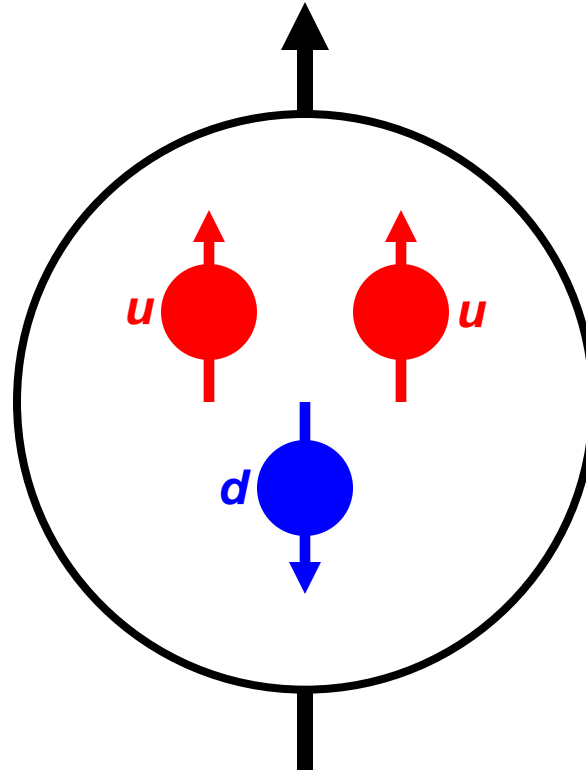
**Carl Gagliardi**

Texas A&M University

## Outline

- Why do we care about the proton spin?
- How do we study it?
- What are we learning?

# The proton in the quark model



- We've known that the proton is made of quarks since the 1960's
- The 2 up quarks and 1 down quark together explain the proton quantum numbers: charge, parity, *spin*, ...
- **Spin** is a particularly useful tool to explore the proton structure because it arises from **intrinsic quantum mechanical dynamics**

# Proton wavefunction in the static quark model

$$\begin{aligned} & \sqrt{\frac{2}{9}} |(u \uparrow)(u \uparrow)(d \downarrow)\rangle - \sqrt{\frac{1}{18}} |(u \uparrow)(u \downarrow)(d \uparrow)\rangle - \sqrt{\frac{1}{18}} |(u \downarrow)(u \uparrow)(d \uparrow)\rangle + \\ & \sqrt{\frac{2}{9}} |(d \downarrow)(u \uparrow)(u \uparrow)\rangle - \sqrt{\frac{1}{18}} |(d \uparrow)(u \uparrow)(u \downarrow)\rangle - \sqrt{\frac{1}{18}} |(d \uparrow)(u \downarrow)(u \uparrow)\rangle + \\ & \sqrt{\frac{2}{9}} |(u \uparrow)(d \downarrow)(u \uparrow)\rangle - \sqrt{\frac{1}{18}} |(u \downarrow)(d \uparrow)(u \uparrow)\rangle - \sqrt{\frac{1}{18}} |(u \uparrow)(d \uparrow)(u \downarrow)\rangle \end{aligned}$$

**x (totally anti-symmetric color wavefunction)**

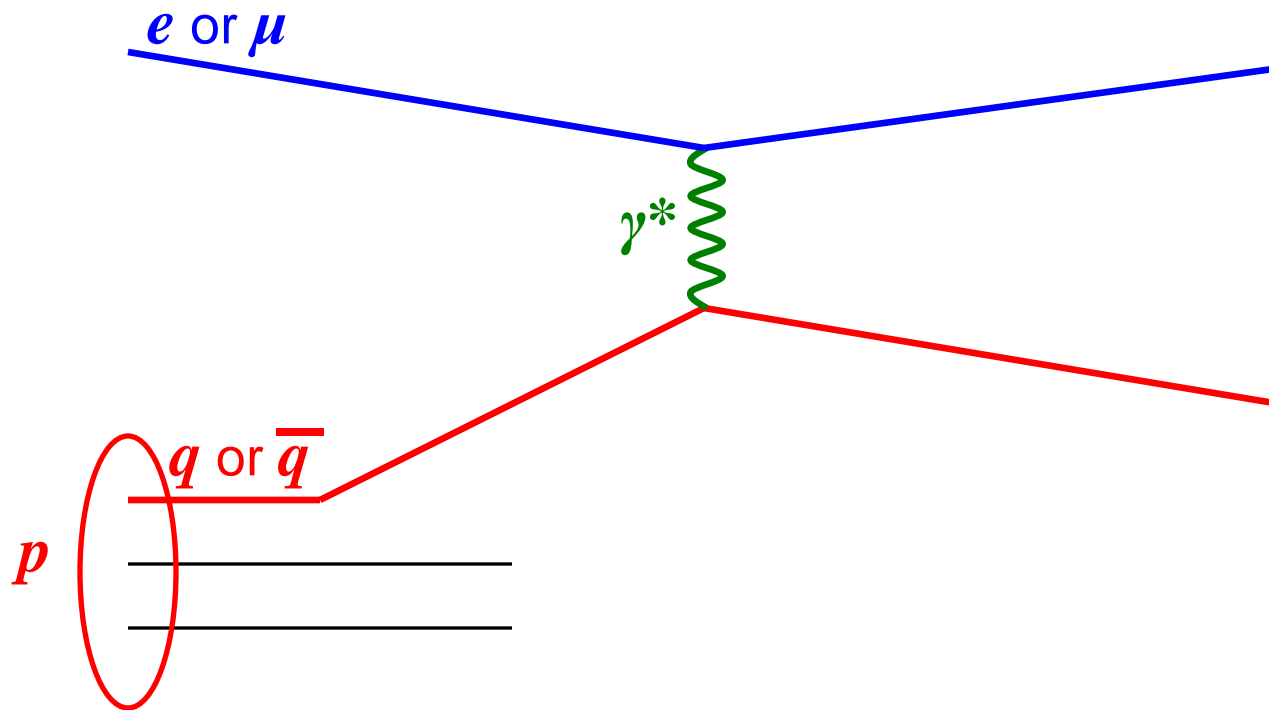
- If  $m_u = m_d = m_p/3$ . Then:
- Proton magnetic moment:
  - Calculate  $+3 \mu_N$ ; find  $+2.793 \mu_N$
- Neutron magnetic moment:
  - Calculate  $-2 \mu_N$ ; find  $-1.913 \mu_N$
- Ratio matches prediction to  $\sim 3\%$

If assume quarks are slightly heavier to allow for some binding energy, can match the observed magnetic moments very well

# Too good to be true

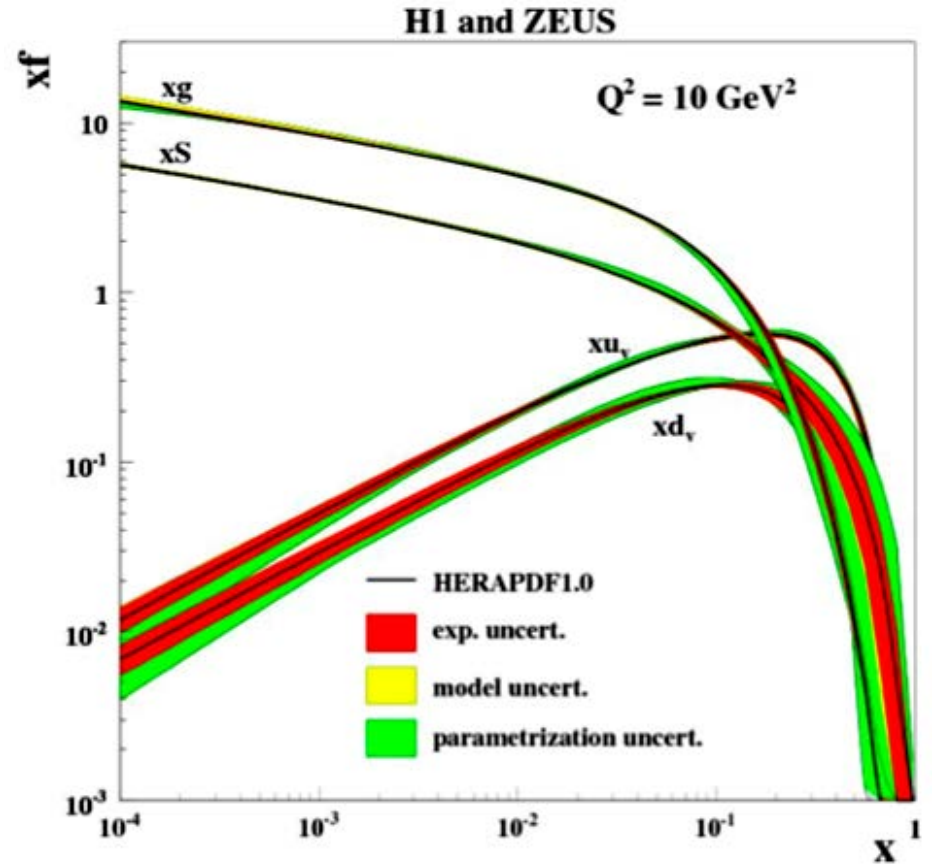
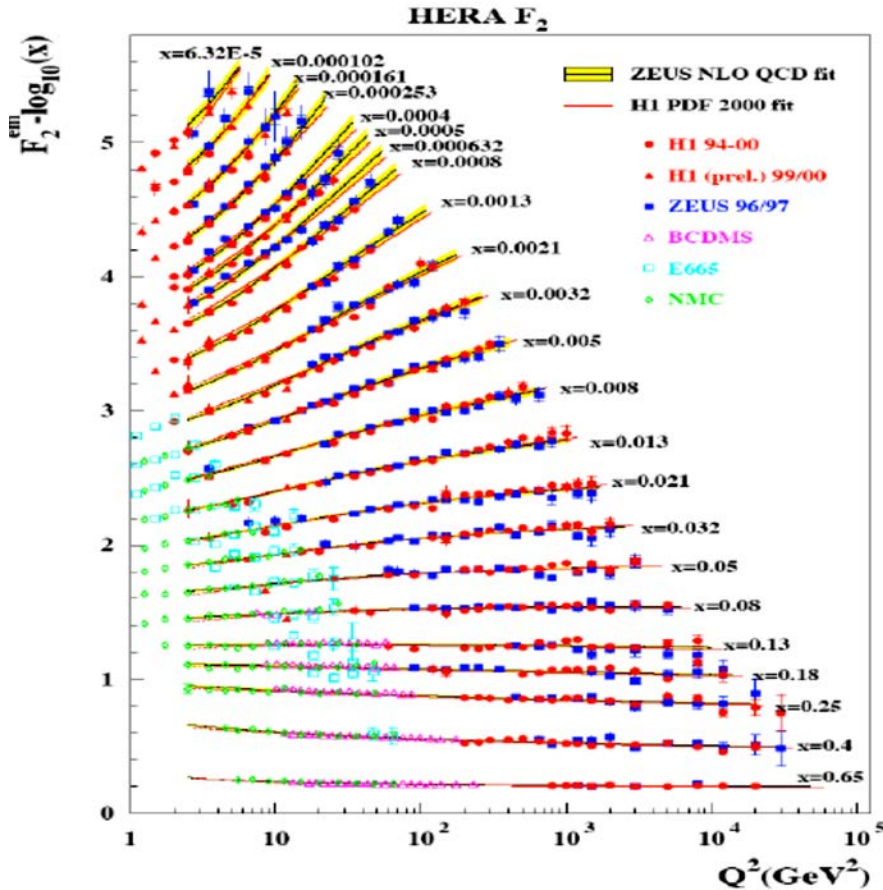
- The proton radius is  $\sim 0.85$  fm
- Heisenberg Uncertainty Principle implies quark motion must be relativistic
- Relativistic quark model
  - Quarks are no longer restricted to *s*-wave states
  - Quark spin accounts for  $\sim 60\%$  of the proton spin
  - Rest of proton spin comes from quark orbital angular momentum
- No binding force in these calculations
- Strong force (**Quantum Chromodynamics**) provides the quark binding
  - Gluons must also be present
  - Can also have additional quark-antiquark pairs
- **How can we observe these quarks, anti-quarks, and gluons?**

# Looking inside the proton



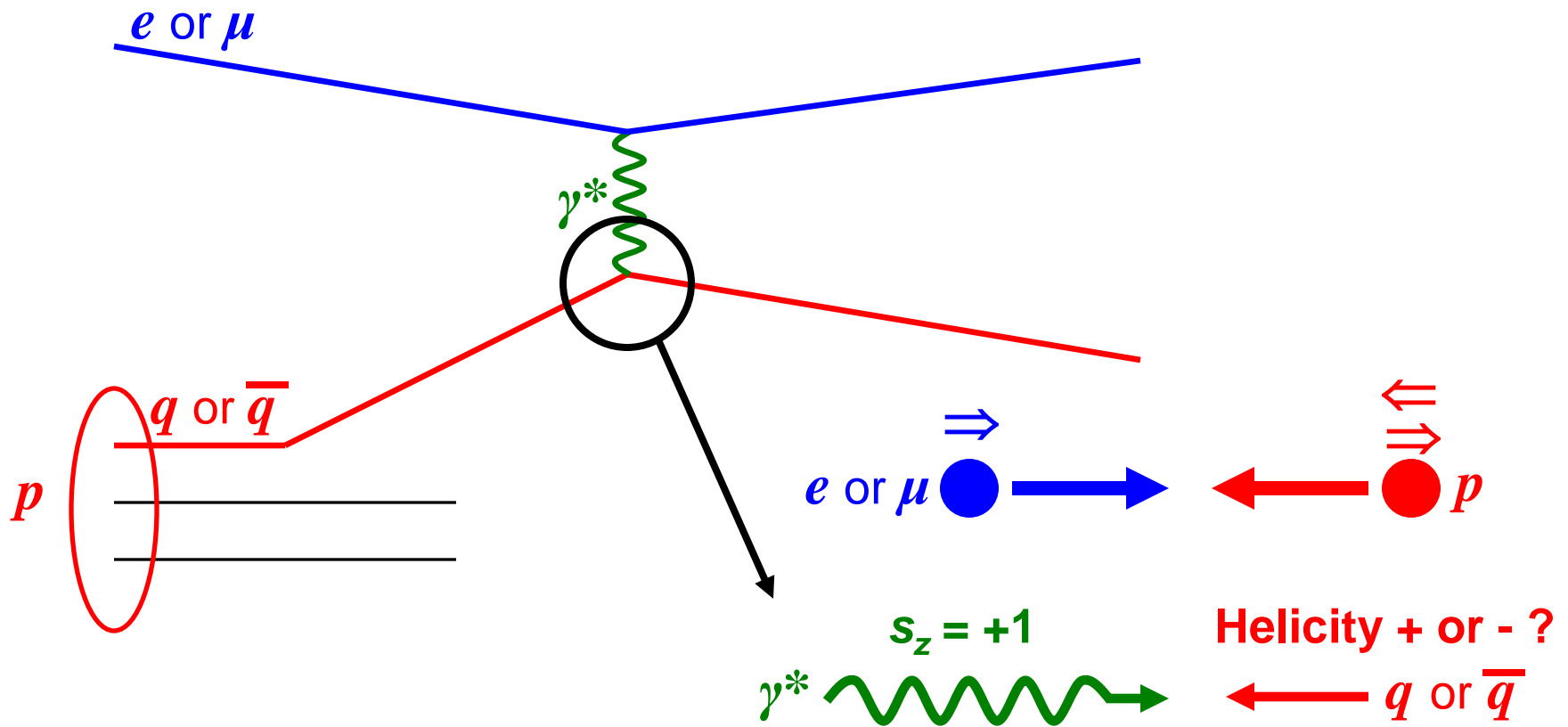
- “Deep-inelastic scattering” (DIS) of electrons and muons off protons has taught us a great deal about the internal structure of the proton
- Interaction is electromagnetic  $\rightarrow$  only quarks and anti-quarks participate directly
- Obtain information about gluons indirectly

# Parton distribution functions



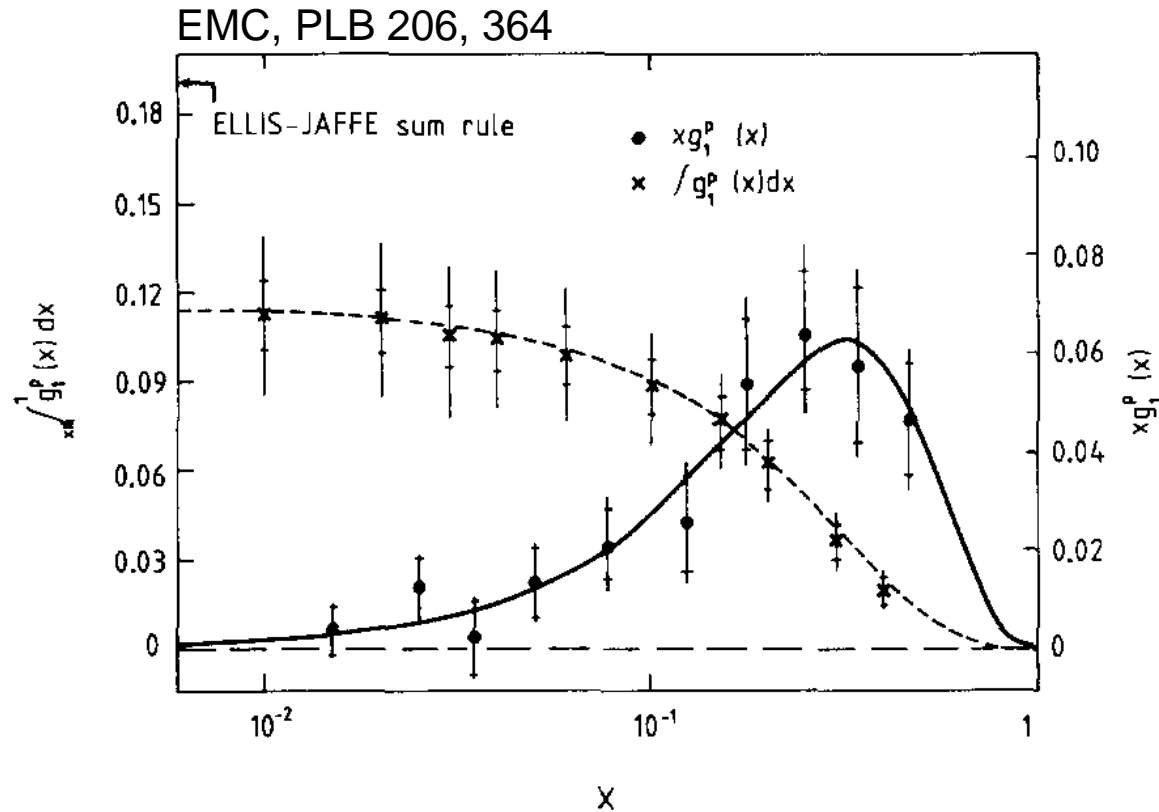
- Probability of finding a quark or gluon inside the proton carrying a fraction  $x$  of the total momentum of the proton
- Find **more gluons** than anything else
- Gluons carry **half the momentum** of the proton

# Microscopic origin of the proton spin



- Measure deep-inelastic scattering with **polarized** electrons or muons off **polarized** protons
- Difference in cross section for like vs. unlike helicity beams provides information about **spin orientations** of the quarks inside the **polarized proton**

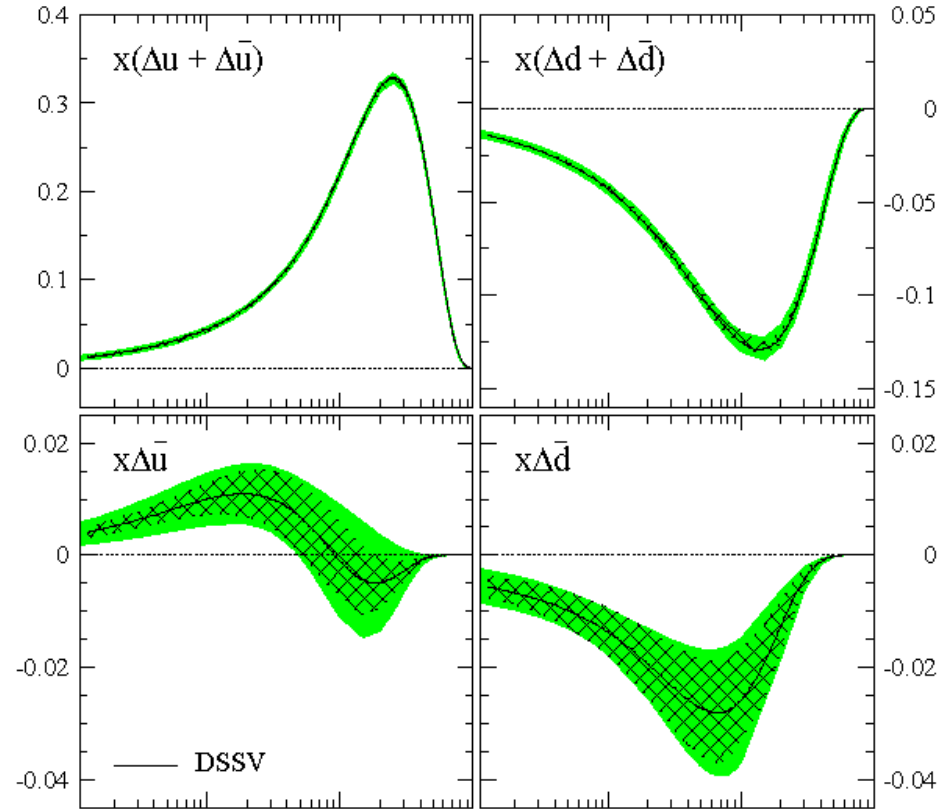
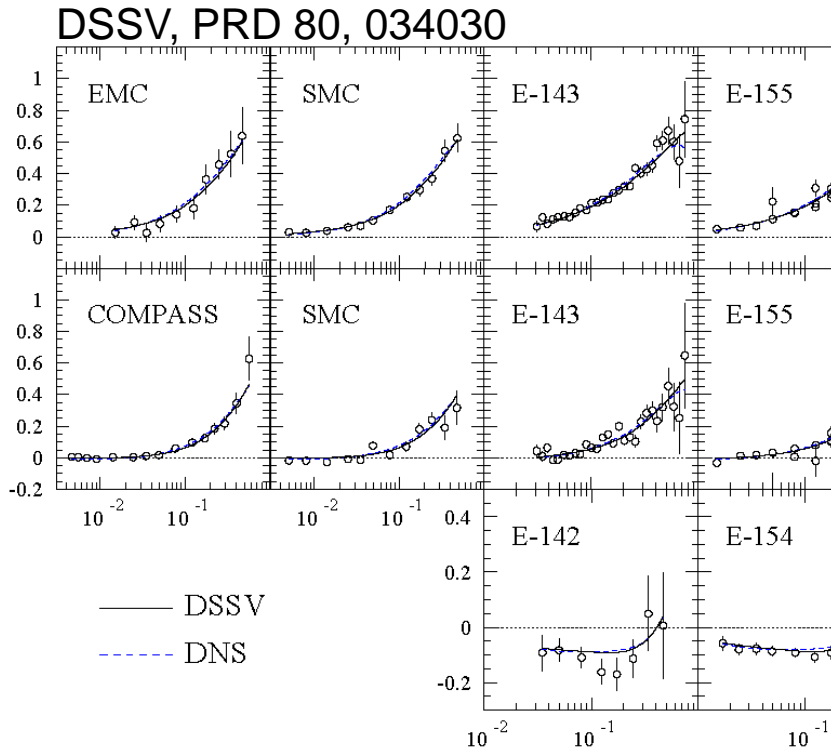
# Proton “spin crisis”



- First measurement over a broad kinematic region was performed by the European Muon Collaboration in the mid-'80s
- Found that quarks contribute only  $(14 \pm 9 \pm 21)\%$  of the proton spin

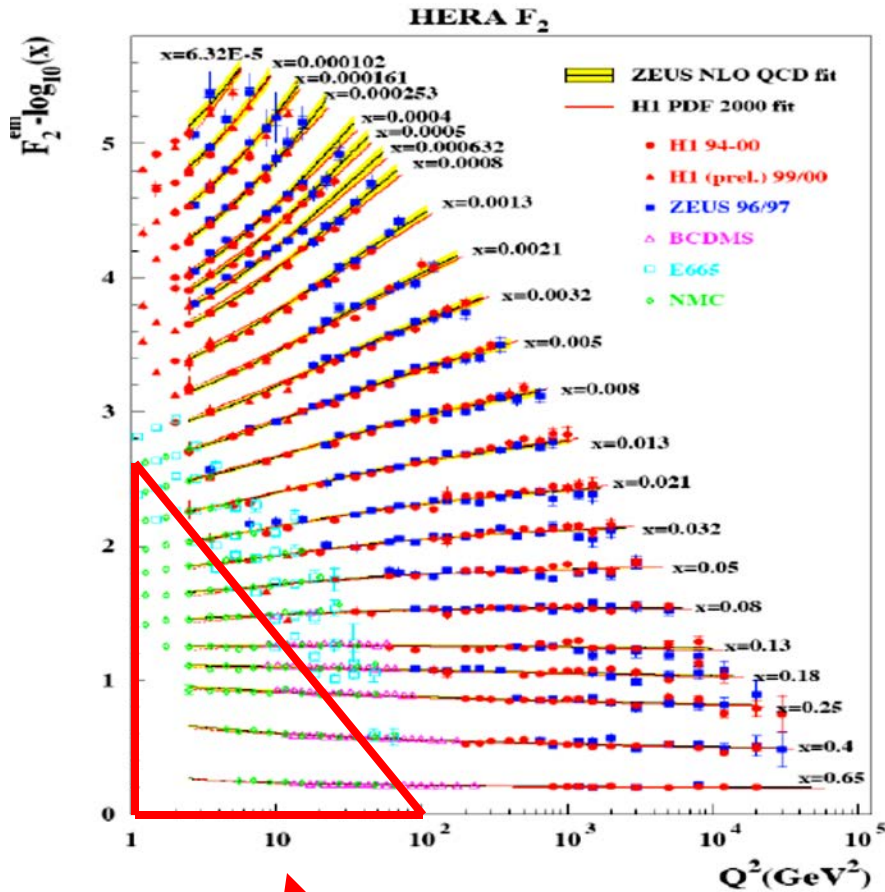


# Since EMC

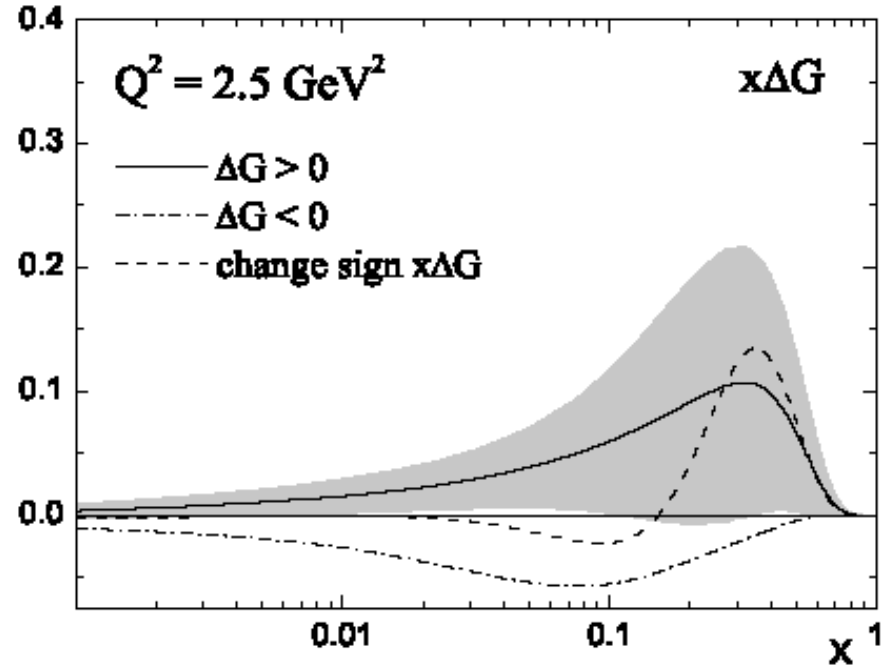


- Many subsequent measurements
- Results are well described by “global analyses” that find best-fit *polarized parton distribution functions*
- Polarization of  $u+\bar{u}$  and  $d+\bar{d}$  quarks well determined
  - Individual  $u, \bar{u}, d, \bar{d}$  polarizations have much larger uncertainty
- Only **~30% of the proton spin** arises from quarks and antiquarks

# What about gluon polarization?



Kinematic region of **polarized** measurements



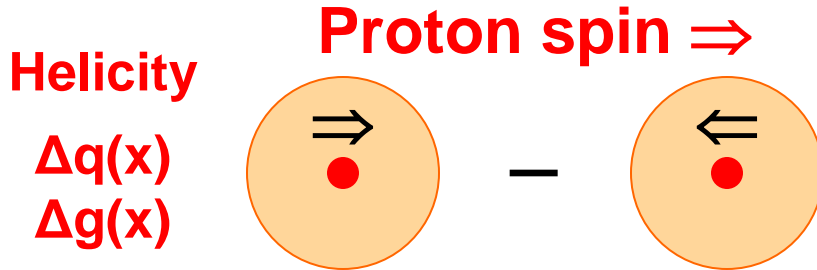
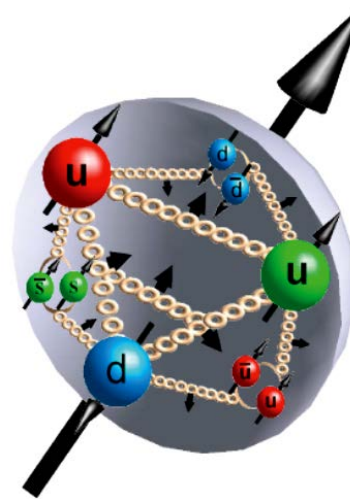
Three fits of equal quality:

- $\Delta G = 0.13 \pm 0.16$
  - $\Delta G \sim 0.006$
  - $\Delta G = -0.20 \pm 0.41$
- all at  $Q^2 = 1 \text{ GeV}^2$

Leader et al, PRD 75, 074027

# What contributes to the proton spin?

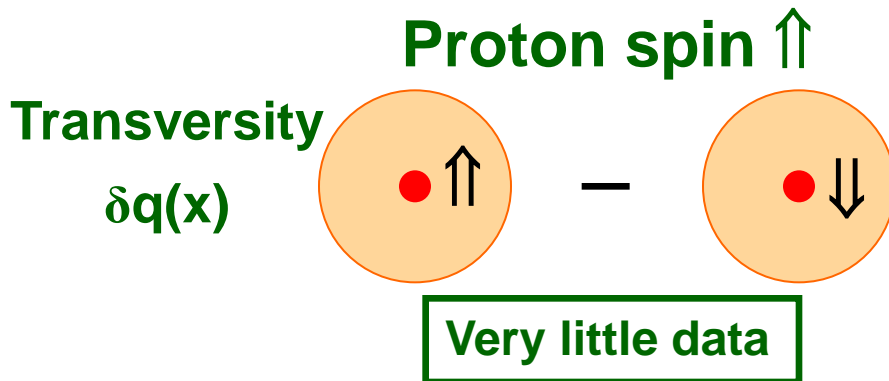
Consider a proton moving toward the right



**Polarized DIS: ~ 0.3**

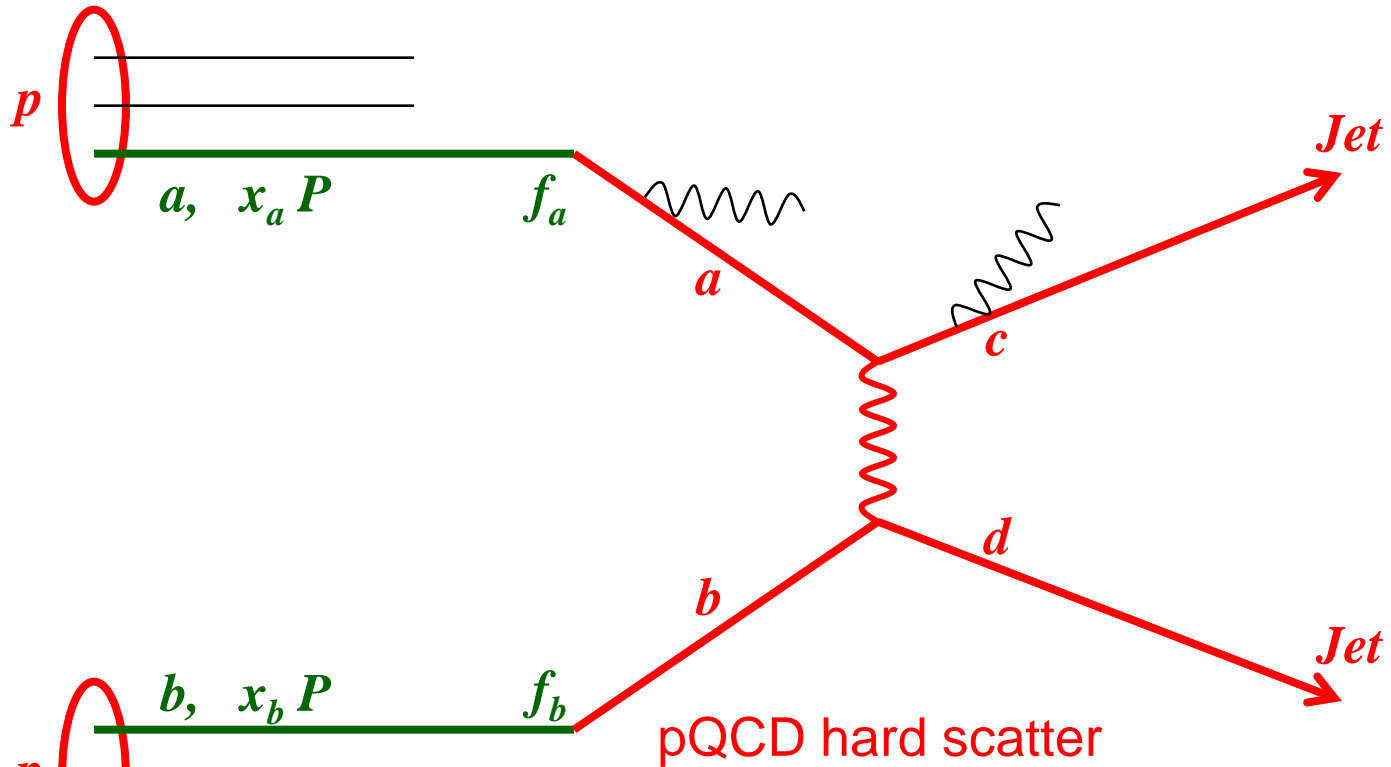
**Poorly constrained**

Spin sum rule:  $\langle S_z^p \rangle = \frac{1}{2} = \frac{1}{2} \Delta \Sigma + \Delta G + \langle L \rangle$



**RHIC spin program:**  
 Exploring poorly determined components of the proton

# $p + p$ collisions in perturbative QCD



$$\sigma = \sum f_a(x_a, Q^2) f_b(x_b, Q^2) \hat{\sigma}_{a+b \rightarrow c+d}$$

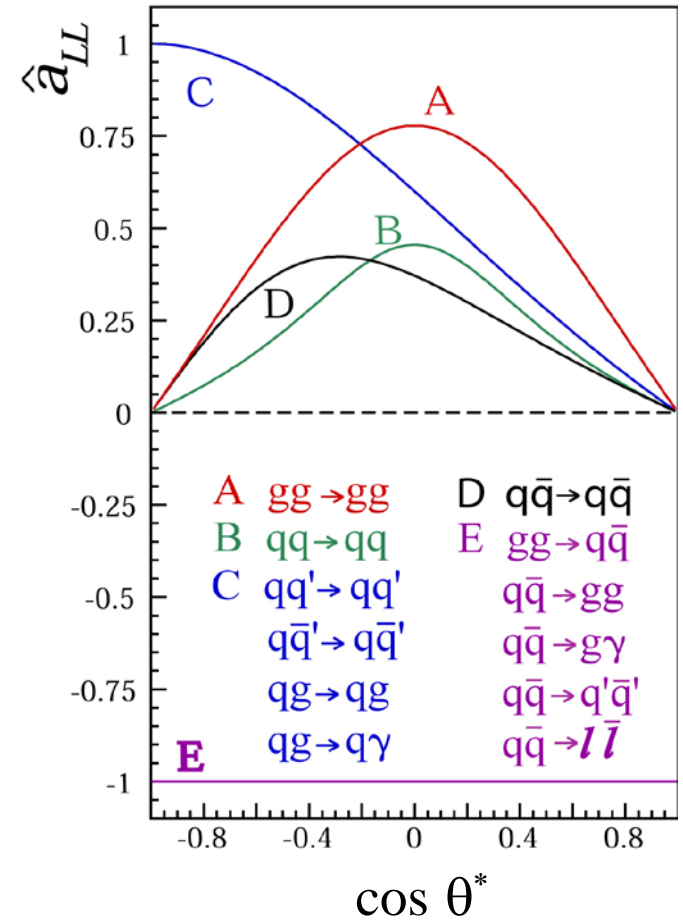
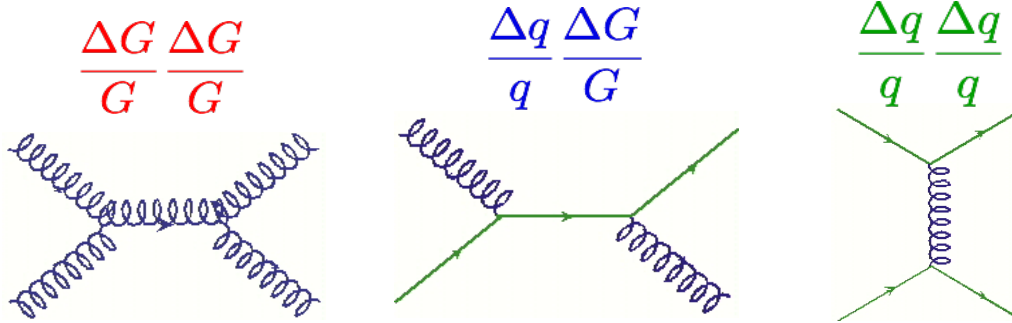
Parton distribution functions

$a$  and  $b$  can be quarks, gluons, or a combination

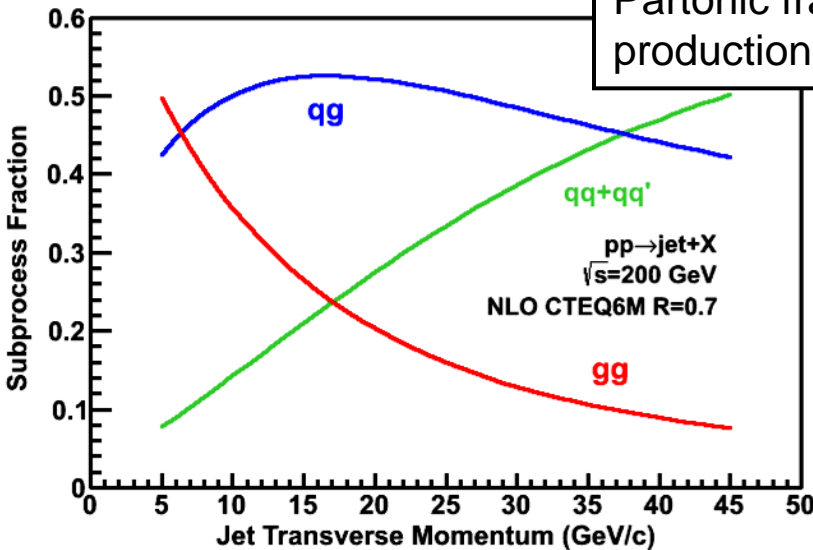
# Exploring gluon polarization at RHIC

$$A_{LL} = \frac{\sigma^{++} - \sigma^{+-}}{\sigma^{++} + \sigma^{+-}} \propto \frac{\Delta f_a \Delta f_b}{f_a f_b} \hat{a}_{LL}$$

$\Delta f$ : polarized parton distribution functions

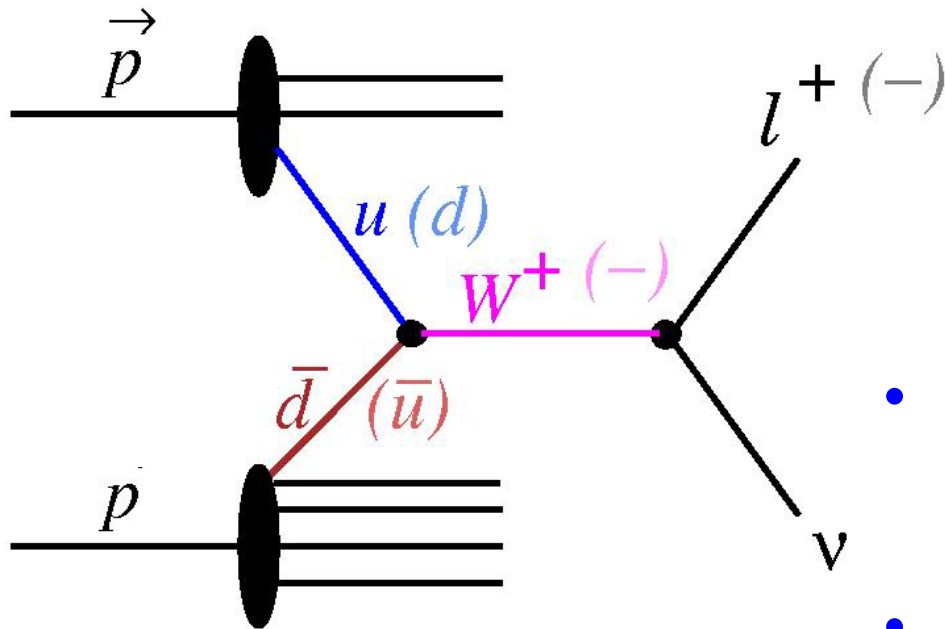


Partonic fractions in jet production at 200 GeV



For most RHIC kinematics, **gg** and **qq** dominate, making  $A_{LL}$  sensitive to **gluon polarization**.

# Separating quark and anti-quark polarizations



$$u + \bar{d} \rightarrow W^+ \rightarrow e^+ + \nu$$

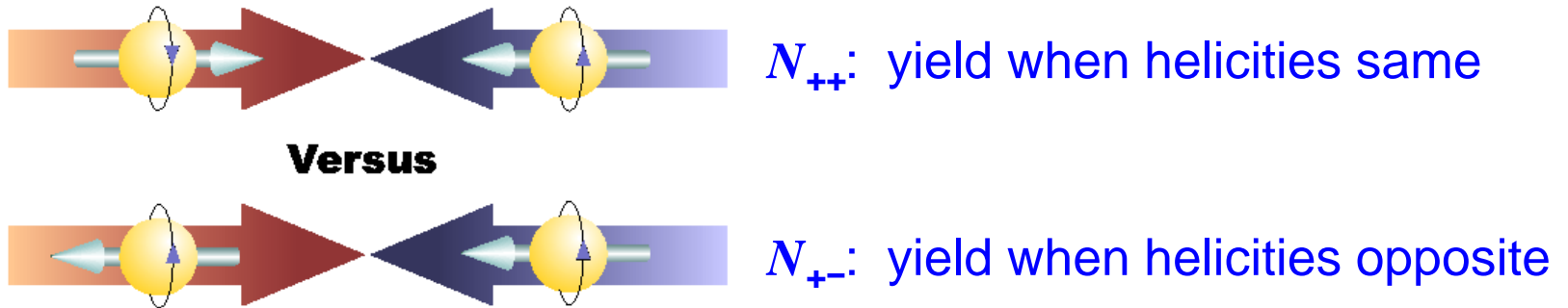
$$\bar{u} + d \rightarrow W^- \rightarrow e^- + \bar{\nu}$$

- Weak interaction process
  - Only left-handed quarks
  - Only right-handed anti-quarks
- Perfect spin separation

Measure parity violating single helicity asymmetry  $A_L$   
 (Helicity flip in one beam while averaging over the other)

$$A_L^{W^-} \propto -\Delta d(x_1)\bar{u}(x_2) + \Delta\bar{u}(x_1)d(x_2) \quad A_L^{W^+} \propto -\Delta u(x_1)\bar{d}(x_2) + \Delta\bar{d}(x_1)u(x_2)$$

# What's needed to determine $A_{LL}$ ?



$$A_{LL} = \frac{1}{P_1 P_2} \frac{N_{++} - RN_{+-}}{N_{++} + RN_{+-}} \quad \text{where} \quad R = \frac{L_{++}}{L_{+-}}$$

- Three concurrent measurements:
  - Beam polarizations
  - Relative luminosities
  - Event yields
- $A_L$  is done similarly, but with one beam polarized and one unpolarized

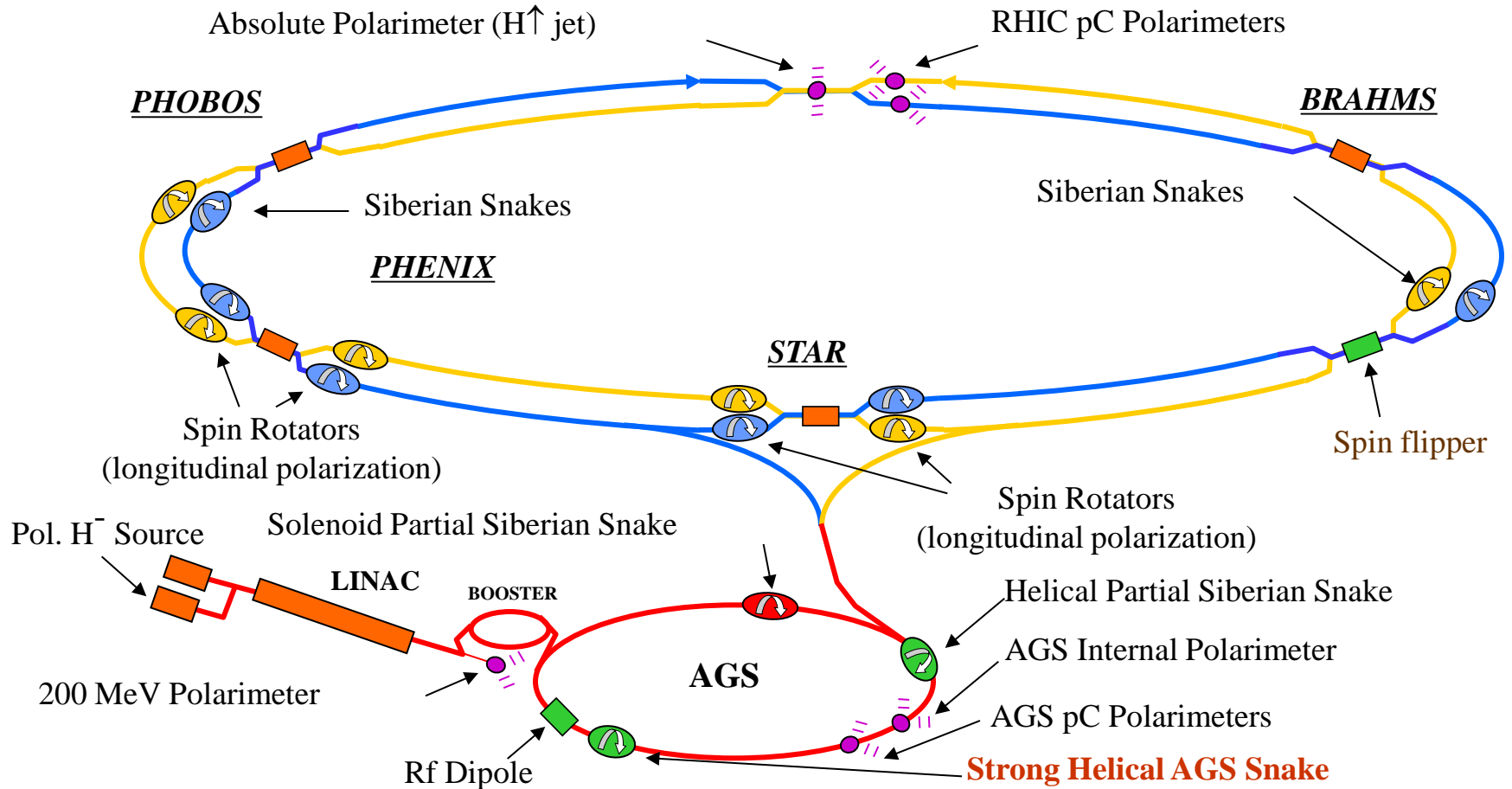
# RHIC: the Relativistic Heavy Ion Collider



- Search for and study the Quark-Gluon Plasma
- **Explore the partonic structure of the proton**
- Determine the partonic structure of nuclei

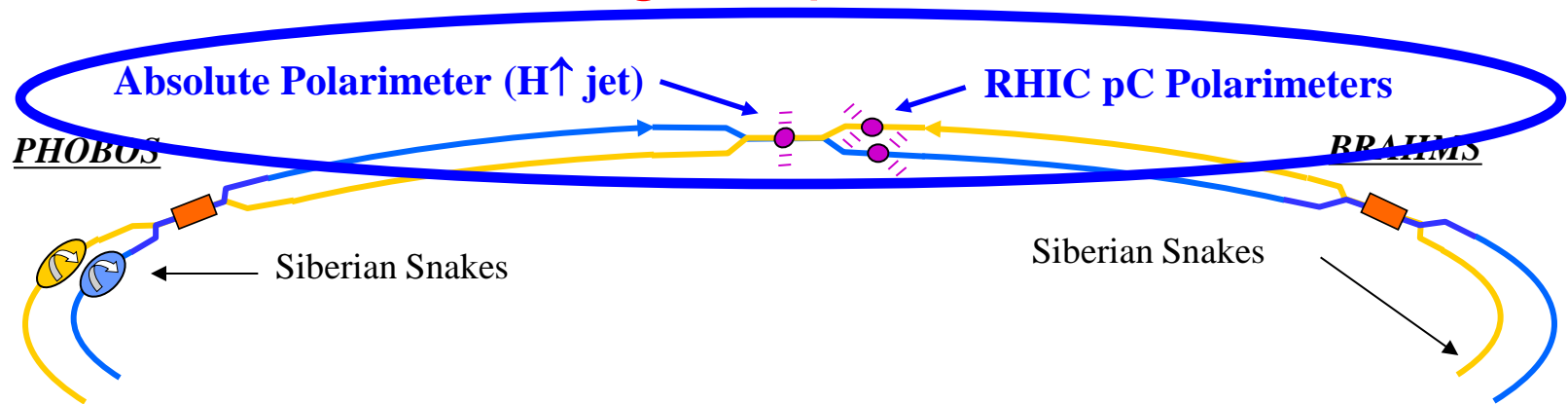


# RHIC: the world's first (and only!) polarized hadron collider



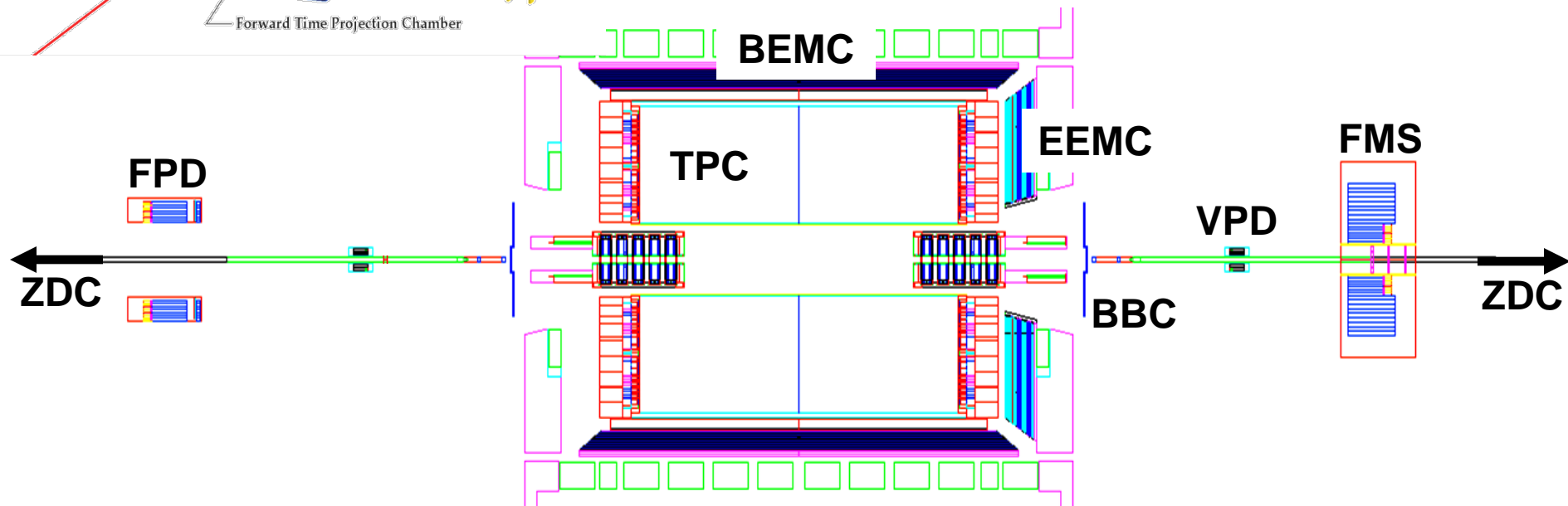
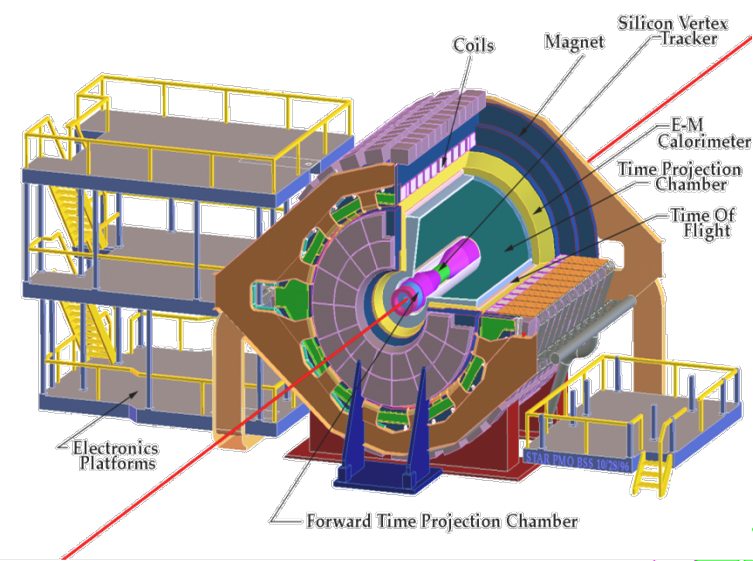
- Spin varies from rf bucket to rf bucket (9.4 MHz)
- Spin pattern changes from fill to fill
- Spin rotators provide choice of spin orientation
- Billions of spin reversals during a fill with little depolarization

# Measuring the polarization



- p-Carbon
  - Quick measurements
  - Determine beam polarization and intensity profiles
  - Multiple measurements give time dependence during a fill
  - Only give relative measurements
- H Jet
  - Circulating beams scatter off a polarized H atomic beam
    - Atomic beam polarization known with high precision
  - Provides absolute determination of the circulating beam polarizations averaged over each fill

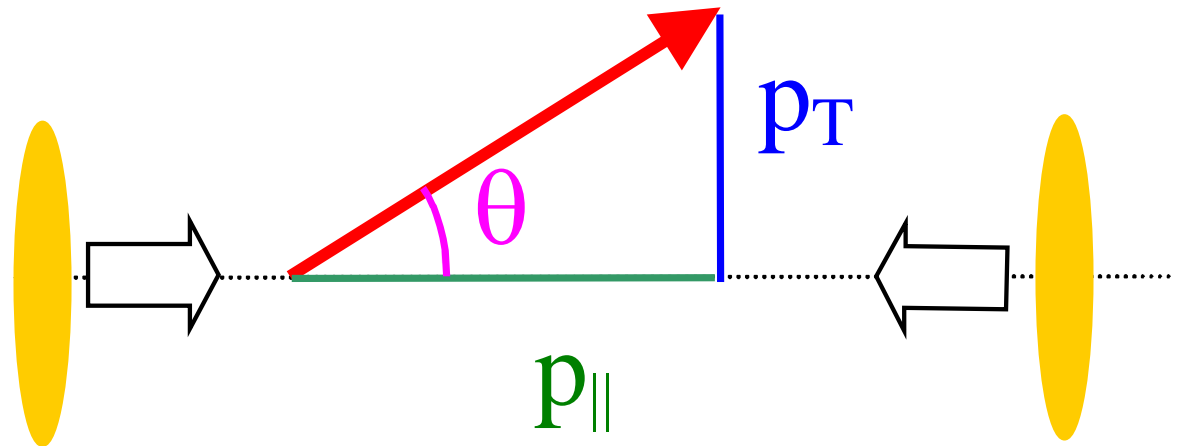
# Event yields and luminosity: the *STAR* detector in two views



- High precision tracking with the TPC
- Electromagnetic calorimetry with the BEMC, EEMC, and FMS
- Additional detectors for relative luminosity, local polarimetry, and minbias triggering

What are we learning?

# Kinematics for colliders



Pseudo-rapidity:  $\eta = -\ln[\tan(\theta/2)]$

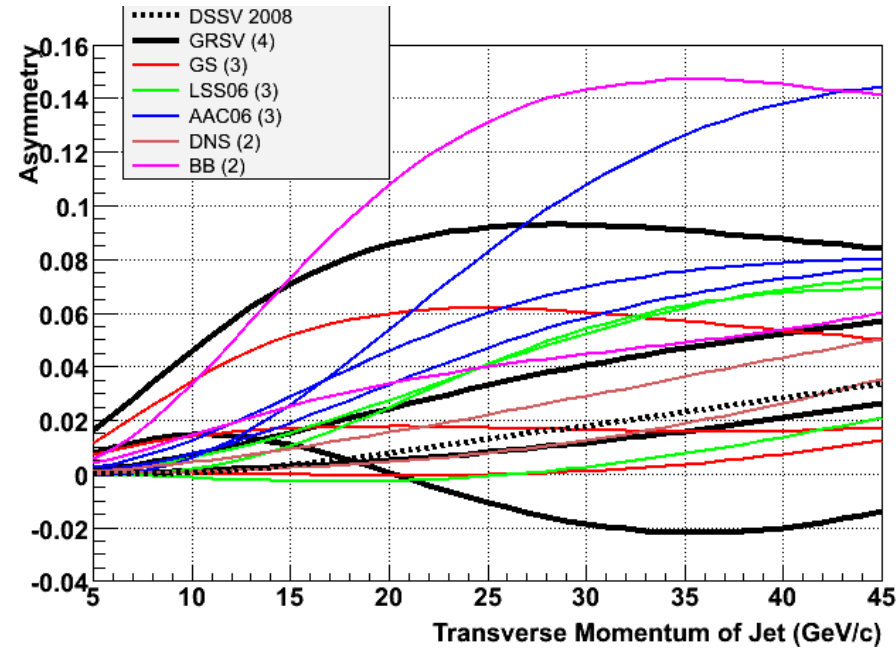
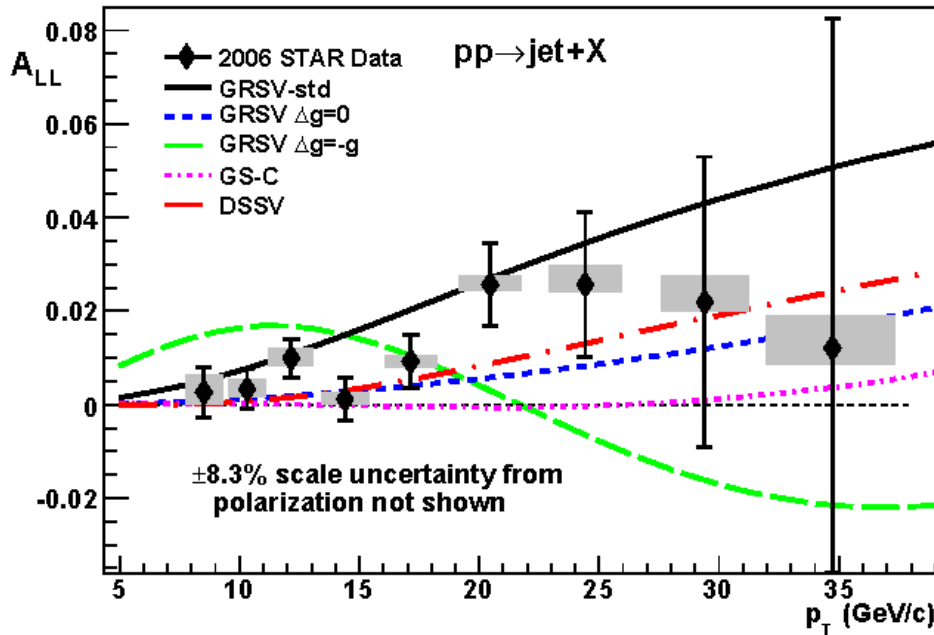
Transverse momentum ( $p_T$ ) and pseudorapidity ( $\eta$ ) provide a convenient description

$$p_z = p_T \sinh(\eta)$$

$$p_{tot} = p_T \cosh(\eta)$$

Mid-rapidity:  $\eta = 0$ , perpendicular to the incident beams  
 $\eta = 1$ : Scattering at  $\theta \sim 40^\circ$  in the CM (or lab) frame  
 $\eta = 2$ : Scattering at  $\theta \sim 15^\circ$  in the CM (or lab) frame

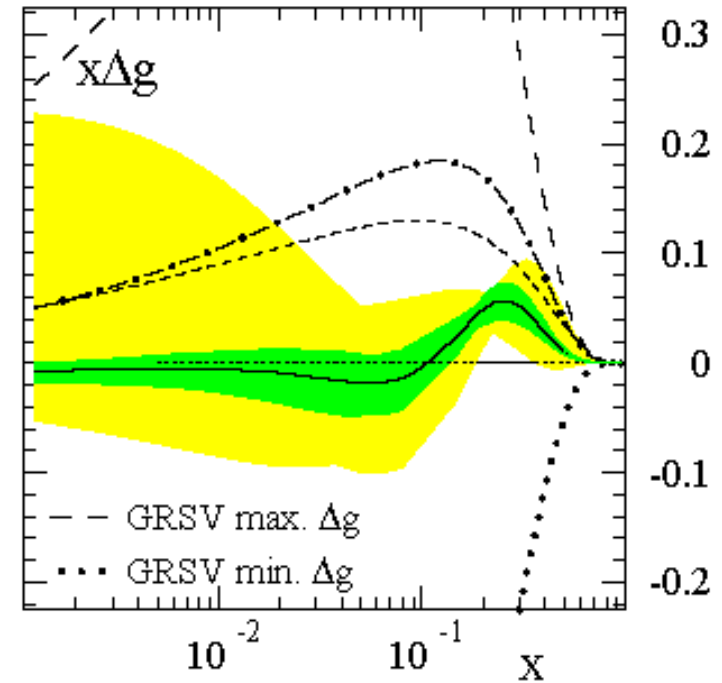
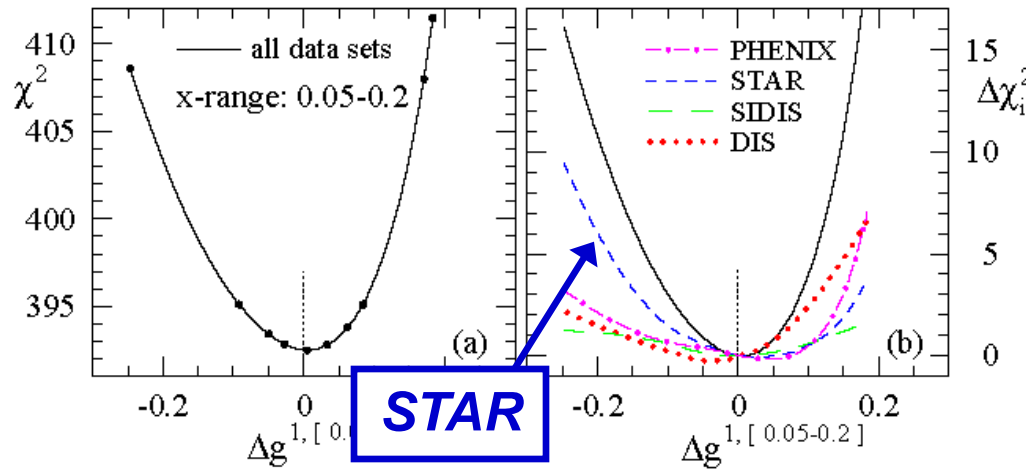
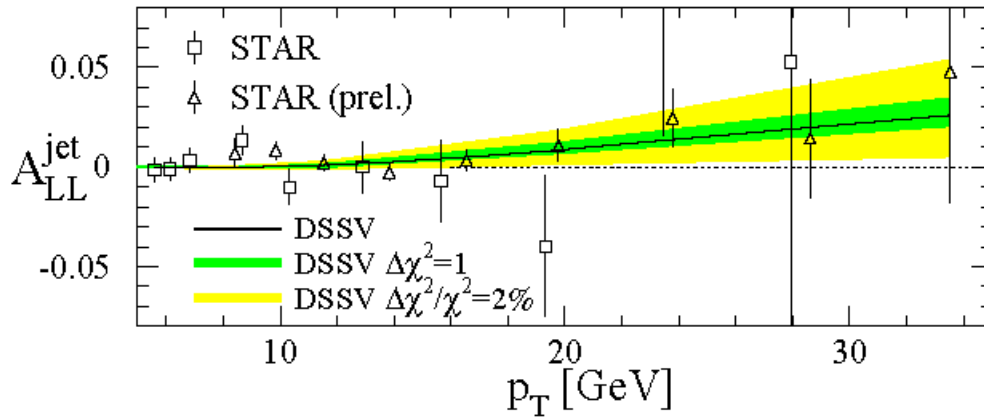
# STAR inclusive jet $A_{LL}$ from 2006



- STAR inclusive jet  $A_{LL}$  excludes those scenarios that have a large gluon polarization within the accessible  $x$  region

# DSSV – first global analysis with polarized jets

de Florian et al., PRL 101, 072001

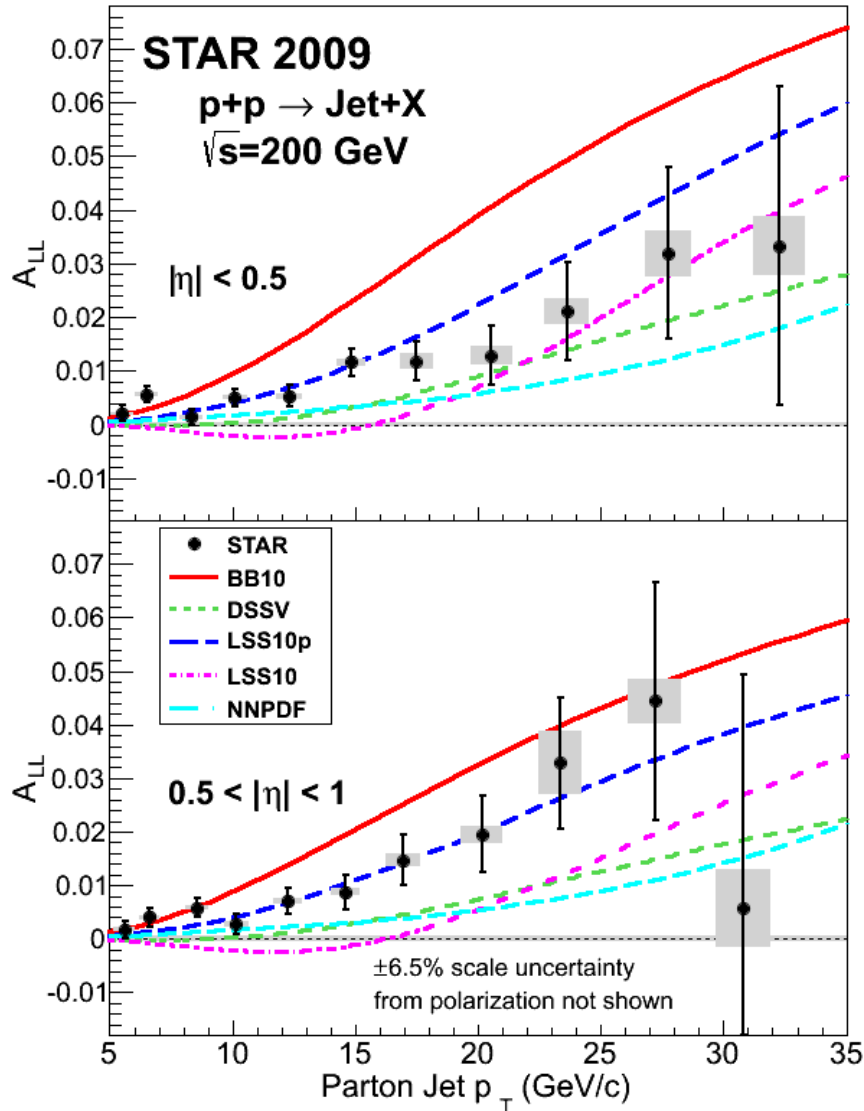


- The first global NLO analysis to include inclusive DIS, SIDIS, and RHIC pp data on an equal footing

# $A_{LL}$ for inclusive jets: 2006 to 2009



arXiv:1405.5134



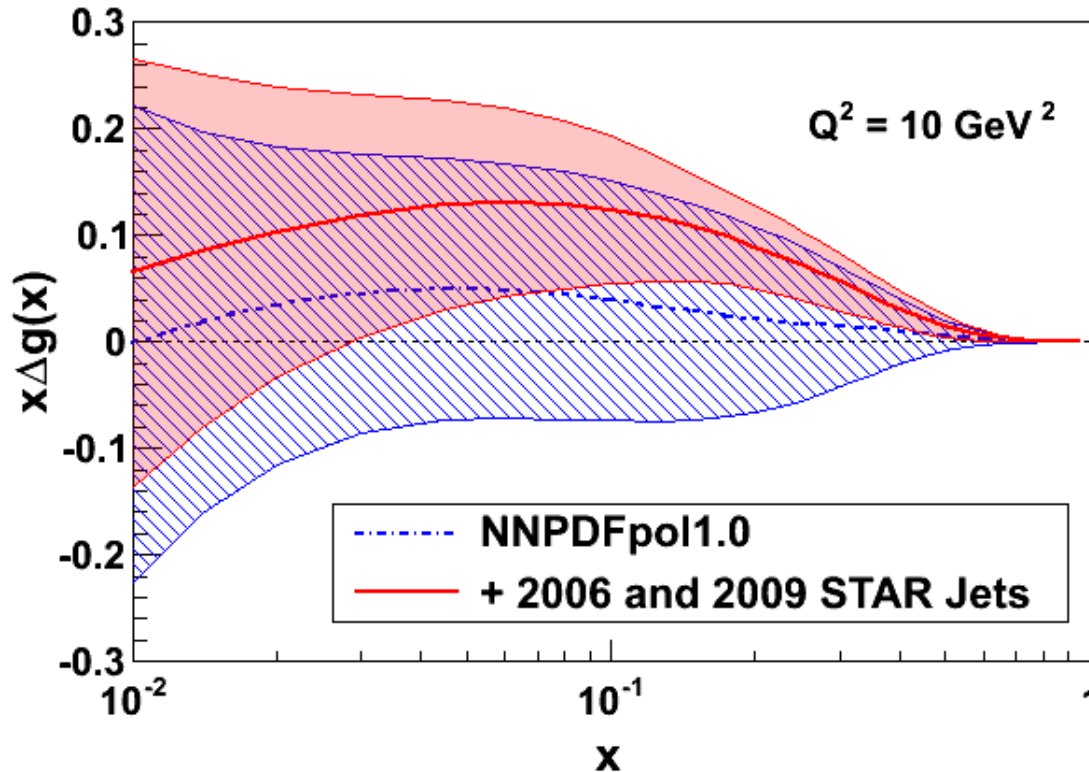
- 20-fold increase in event statistics
- Improved analysis procedures lead to smaller systematic uncertainties
- 2009 **STAR** inclusive jet  $A_{LL}$  measurements are a factor of 3 (high- $p_T$ ) to >4 (low- $p_T$ ) more precise than 2006
- **Measured asymmetries are larger than predictions from DSSV**
  - Points to a **larger gluon polarization**



# STAR inclusive jets and NNPDF



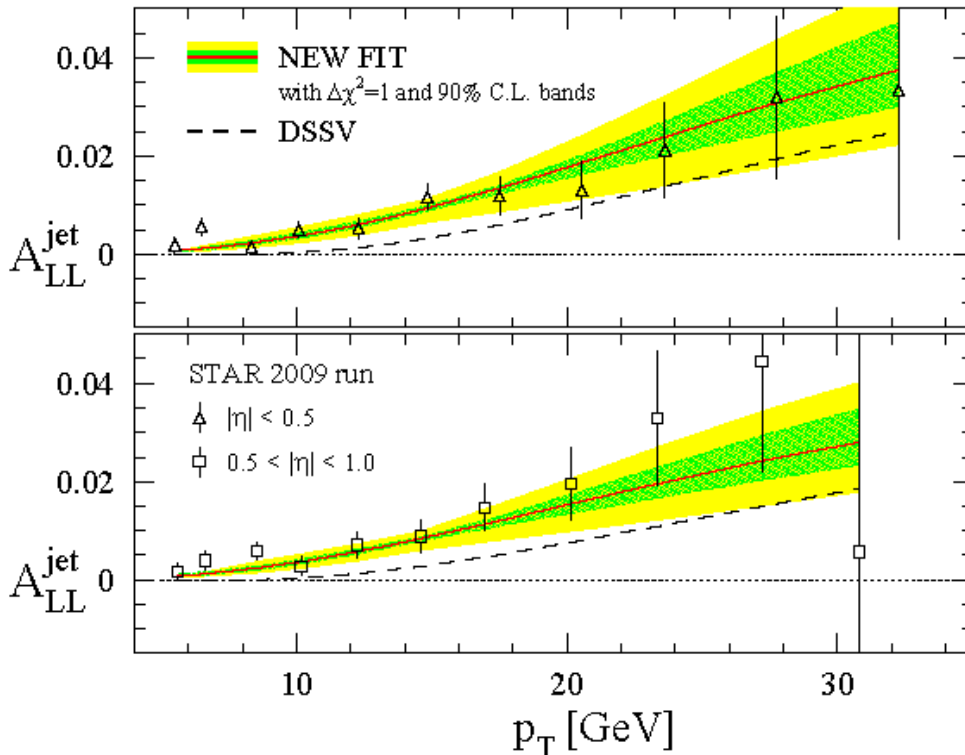
arXiv:1405.5134



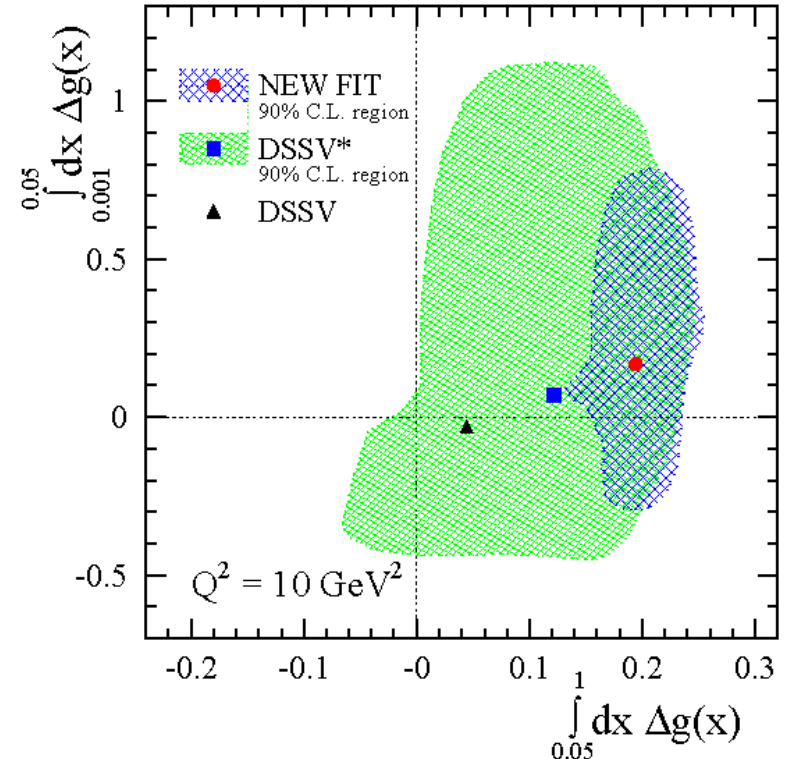
- Included STAR inclusive jet  $A_{LL}$  results in NNPDF via reweighting
- Gluon polarization shifts positive, with much reduced uncertainties
- Integral of  $\Delta g(x, Q^2 = 10 \text{ GeV}^2)$  over the range  $0.05 < x < 0.5$  increases from  $0.06 \pm 0.18$  to  **$0.21 \pm 0.10$**
- Preference for the **gluon helicity contribution to be positive** in the RHIC kinematic range

# STAR inclusive jets and DSSV

DSSV, arXiv:1404.4293



DSSV, arXiv:1404.4293



- **New DSSV global analysis** that includes 2009  $A_{LL}$  measurements from PHENIX and STAR

$$\int_{0.05}^1 \Delta g(x, Q^2 = 10 \text{ GeV}^2) dx = 0.20_{-0.07}^{+0.06} \quad \text{at 90\% CL}$$

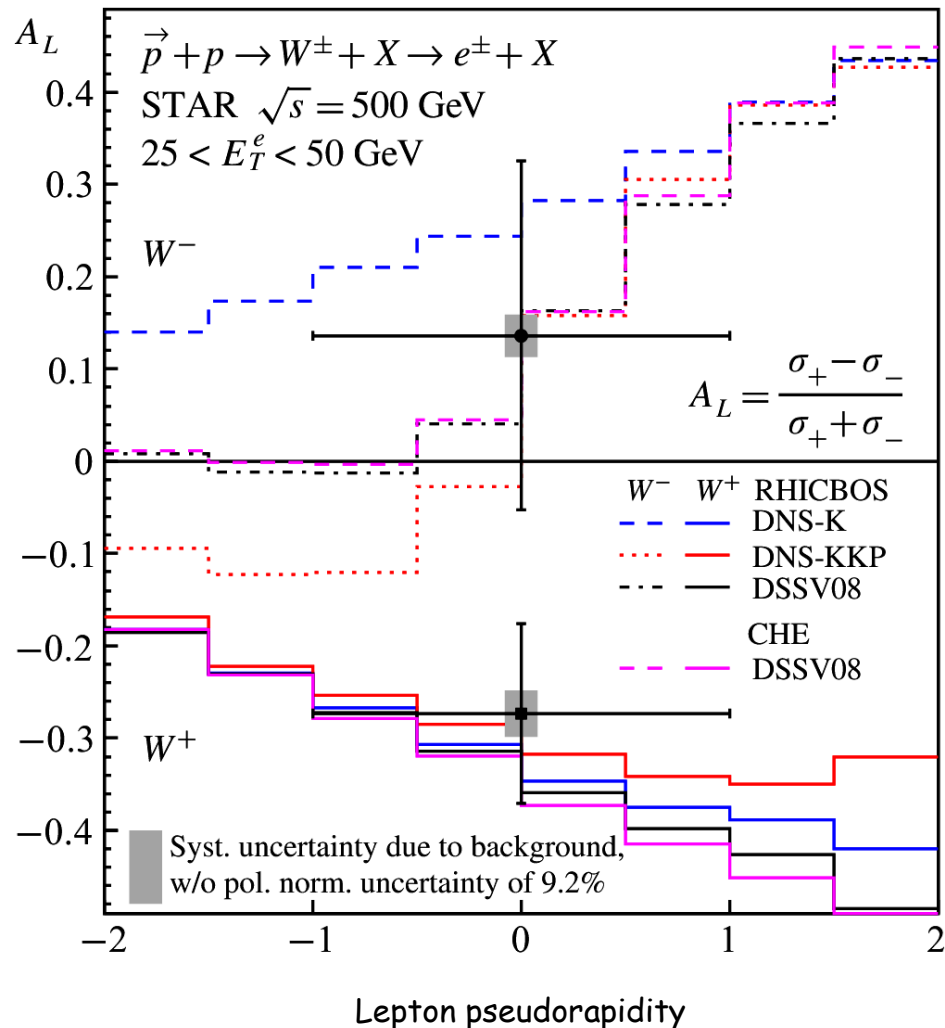
- **STAR jets provide evidence of positive gluon polarization** in the range  $x > 0.05$

# You in a few months?

## Precision Measurement of the Longitudinal Double-spin Asymmetry for Inclusive Jet Production in Polarized Proton Collisions at $\sqrt{s} = 200$ GeV

L. Adamczyk,<sup>1</sup> J. K. Adkins,<sup>23</sup> G. Agakishiev,<sup>21</sup> M. M. Aggarwal,<sup>35</sup> Z. Ahammed,<sup>53</sup> I. Alekseev,<sup>19</sup> J. Alford,<sup>22</sup> C. D. Anson,<sup>32</sup> A. Aparin,<sup>21</sup> D. Arkhipkin,<sup>4</sup> E. C. Aschenauer,<sup>4</sup> G. S. Averichev,<sup>21</sup> A. Banerjee,<sup>53</sup> D. R. Beavis,<sup>4</sup> R. Bellwied,<sup>49</sup> A. Bhasin,<sup>20</sup> A. K. Bhati,<sup>35</sup> P. Bhattarai,<sup>48</sup> H. Bichsel,<sup>55</sup> J. Bielcik,<sup>13</sup> J. Bielcikova,<sup>14</sup> L. C. Bland,<sup>4</sup> I. G. Bordyuzhin,<sup>19</sup> W. Borowski,<sup>45</sup> J. Bouchet,<sup>22</sup> A. V. Brandin,<sup>30</sup> S. G. Brovko,<sup>6</sup> S. Bültmann,<sup>33</sup> I. Bunzarov,<sup>21</sup> T. P. Burton,<sup>4</sup> J. Butterworth,<sup>41</sup> H. Caines,<sup>57</sup> M. Calderón de la Barca Sánchez,<sup>6</sup> J. M. Campbell,<sup>32</sup> D. Cebra,<sup>6</sup> R. Cendejas,<sup>36</sup> M. C. Cervantes,<sup>47</sup> P. Chaloupka,<sup>13</sup> Z. Chang,<sup>47</sup> S. Chattopadhyay,<sup>53</sup> H. F. Chen,<sup>42</sup> J. H. Chen,<sup>44</sup> L. Chen,<sup>9</sup> J. Cheng,<sup>50</sup> M. Cherney,<sup>12</sup> A. Chikanian,<sup>57</sup> W. Christie,<sup>4</sup> J. Chwastowski,<sup>11</sup> M. J. M. Codrington,<sup>48</sup> G. Contin,<sup>26</sup> J. G. Cramer,<sup>55</sup> H. J. Crawford,<sup>5</sup> A. B. Cudd,<sup>47</sup> L. Cui,<sup>42</sup> S. Das,<sup>16</sup> A. Davila Leyva,<sup>48</sup> L. C. De Silva,<sup>12</sup> R. R. Debbé,<sup>4</sup> T. G. Dedovich,<sup>21</sup> J. Deng,<sup>48</sup> A. A. Derevschikov,<sup>37</sup> R. Derradi de Souza,<sup>8</sup> S. Dhamija,<sup>18</sup> B. di Ruzza,<sup>4</sup> L. Didenko,<sup>4</sup> C. Dilks,<sup>36</sup> F. Ding,<sup>6</sup> P. Djawotho,<sup>47</sup> X. Dong,<sup>26</sup> J. L. Drachenberg,<sup>52</sup> J. E. Draper,<sup>6</sup> C. M. Du,<sup>25</sup> L. E. Dunkelberger,<sup>7</sup> J. C. Dunlop,<sup>4</sup> L. G. Efimov,<sup>21</sup> J. Engelage,<sup>5</sup> K. S. Engle,<sup>51</sup> G. Eppley,<sup>41</sup> L. Eun,<sup>26</sup> O. Evdokimov,<sup>10</sup> O. Eyser,<sup>4</sup> R. Fatemi,<sup>23</sup> S. Fazio,<sup>4</sup> J. Fedorisin,<sup>21</sup> P. Filip,<sup>21</sup> E. Finch,<sup>57</sup> Y. Fisyak,<sup>4</sup> C. E. Flores,<sup>6</sup> C. A. Gagliardi,<sup>47</sup> D. R. Gangadharan,<sup>32</sup> D. Garand,<sup>38</sup> F. Geurts,<sup>41</sup> A. Gibson,<sup>52</sup> M. Girard,<sup>54</sup> S. Gliske,<sup>2</sup> L. Greiner,<sup>26</sup> D. Grosnick,<sup>52</sup> D. S. Gunarathne,<sup>46</sup> Y. Guo,<sup>42</sup> A. Gupta,<sup>20</sup> S. Gupta,<sup>20</sup> W. Guryn,<sup>4</sup> B. Haag,<sup>6</sup> A. Hamed,<sup>47</sup> L.-X. Han,<sup>44</sup> R. Haque,<sup>31</sup> J. W. Harris,<sup>57</sup> S. Heppelmann,<sup>36</sup> A. Hirsch,<sup>38</sup> G. W. Hoffmann,<sup>48</sup> D. J. Hofman,<sup>10</sup> S. Horvat,<sup>57</sup> B. Huang,<sup>4</sup> H. Z. Huang,<sup>7</sup> X. Huang,<sup>50</sup> P. Huck,<sup>9</sup> T. J. Humanic,<sup>32</sup> G. Igo,<sup>7</sup> W. W. Jacobs,<sup>18</sup> H. Jang,<sup>24</sup> E. G. Judd,<sup>5</sup> S. Kabana,<sup>45</sup> D. Kalinkin,<sup>19</sup> K. Kang,<sup>50</sup>

# First STAR $W A_L$



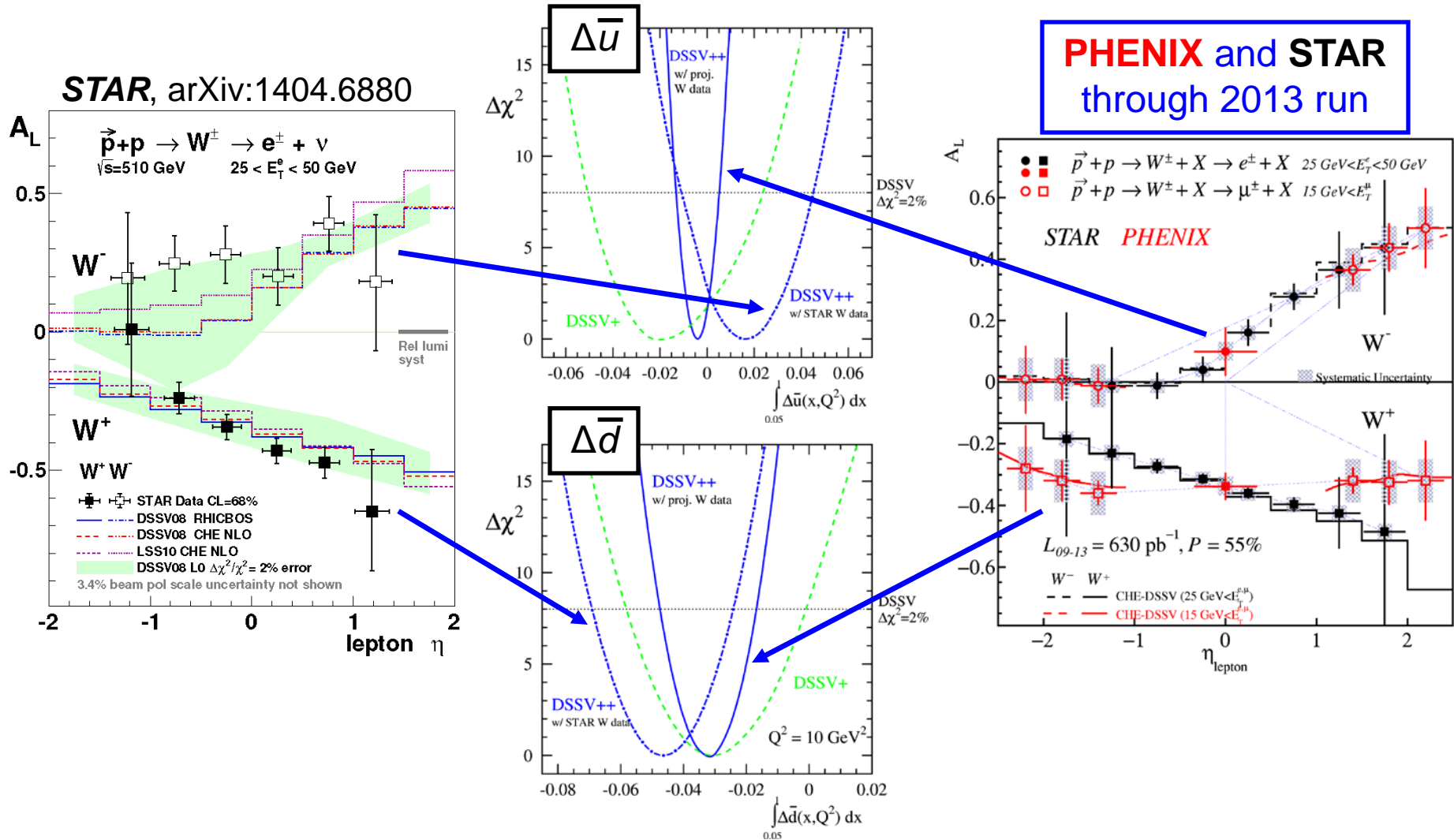
$$A_L = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

## STAR 2009 Result

$$A_L(W^+) = -0.27 \pm 0.10(stat) \pm 0.02(syst)$$

$$A_L(W^-) = 0.14 \pm 0.19(stat) \pm 0.02(syst)$$

# High precision $W$ asymmetry era



- Results from 2011 and 2012 already provide substantial sensitivity
- Future results will provide a dramatic reduction in the uncertainties

# Conclusions

- We still have a great deal to learn about the structure of the proton
- **RHIC is making significant contributions** to three poorly constrained pieces of the puzzle
  - **Gluon polarization**
    - May contribute as much or more to the proton spin as the quarks and anti-quarks
  - **Flavor-separated quark and anti-quark polarizations**
  - **Transversity**
- Still more data have been **recorded and are being analyzed** at this moment. **Stay tuned!**